

# Between Wedge and Window:

An improved point-source foreground  
model for the EoR.

STEVEN MURRAY, ICRAR/CURTIN + CAASTRO,  
PERTH, AUSTRALIA.

... WITH CATH TROTT AND CHRIS JORDAN.



CAASTRO  
ARC CENTRE OF EXCELLENCE  
FOR ALL-SKY ASTROPHYSICS

# Basis of this talk



DRAFT VERSION JULY 3, 2017

Preprint typeset using L<sup>A</sup>T<sub>E</sub>X style emulateapj v. 01/23/15

## AN IMPROVED STATISTICAL POINT-SOURCE FOREGROUND MODEL FOR THE EPOCH OF REIONIZATION

S. G. MURRAY<sup>1,2</sup>, C. M. TROTT<sup>1,2</sup> AND C. H. JORDAN<sup>1,2</sup>

*Draft version July 3, 2017*

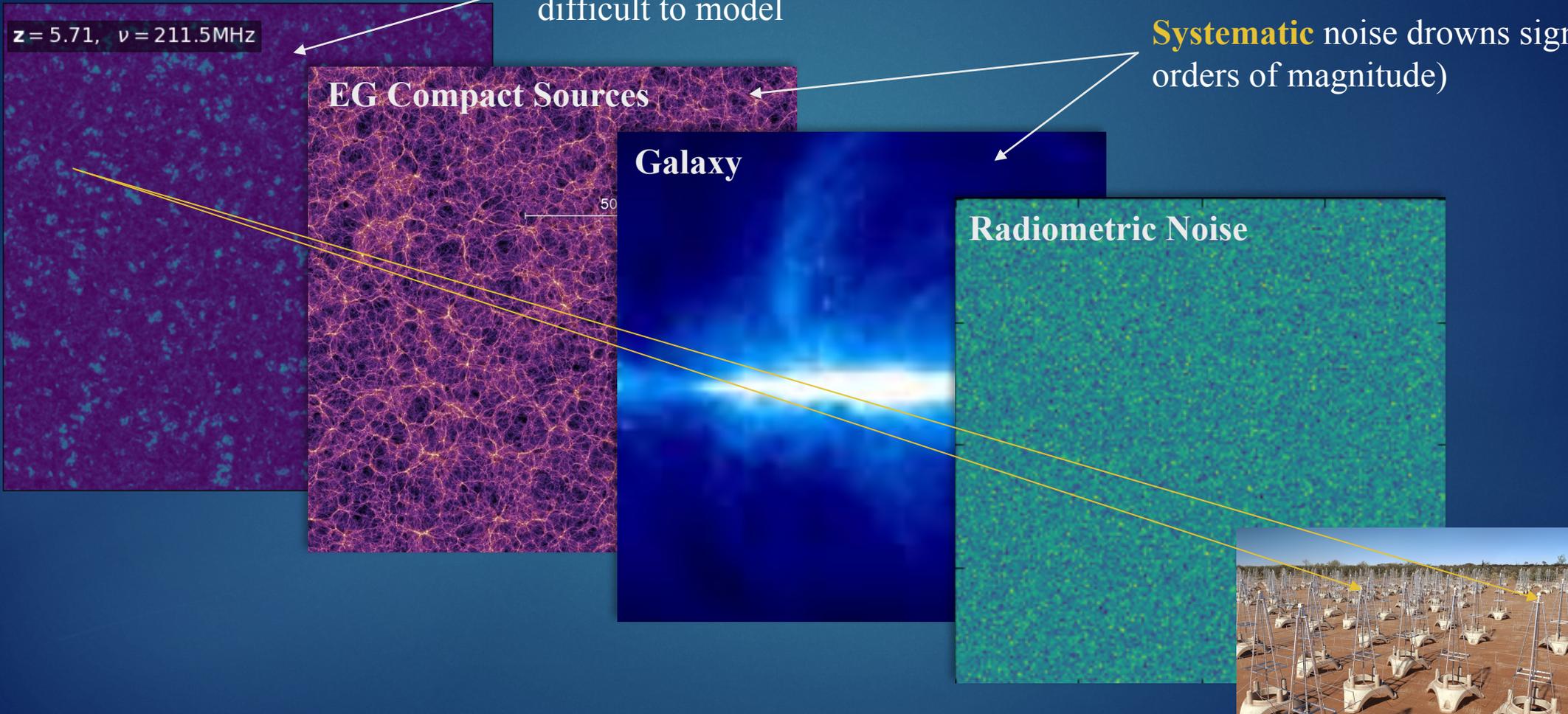
### ABSTRACT

We present a sophisticated statistical point-source foreground model for low-frequency radio Epoch of Reionization (EoR) experiments using the 21 cm neutral hydrogen emission line. Motivated by

# The Challenge of the EoR

Complex astrophysics makes signal difficult to model

**Systematic** noise drowns signal (~4 orders of magnitude)



# The 2D Power Spectrum and Foreground

## Suppression

Most experiments try to detect the **1D PS**.

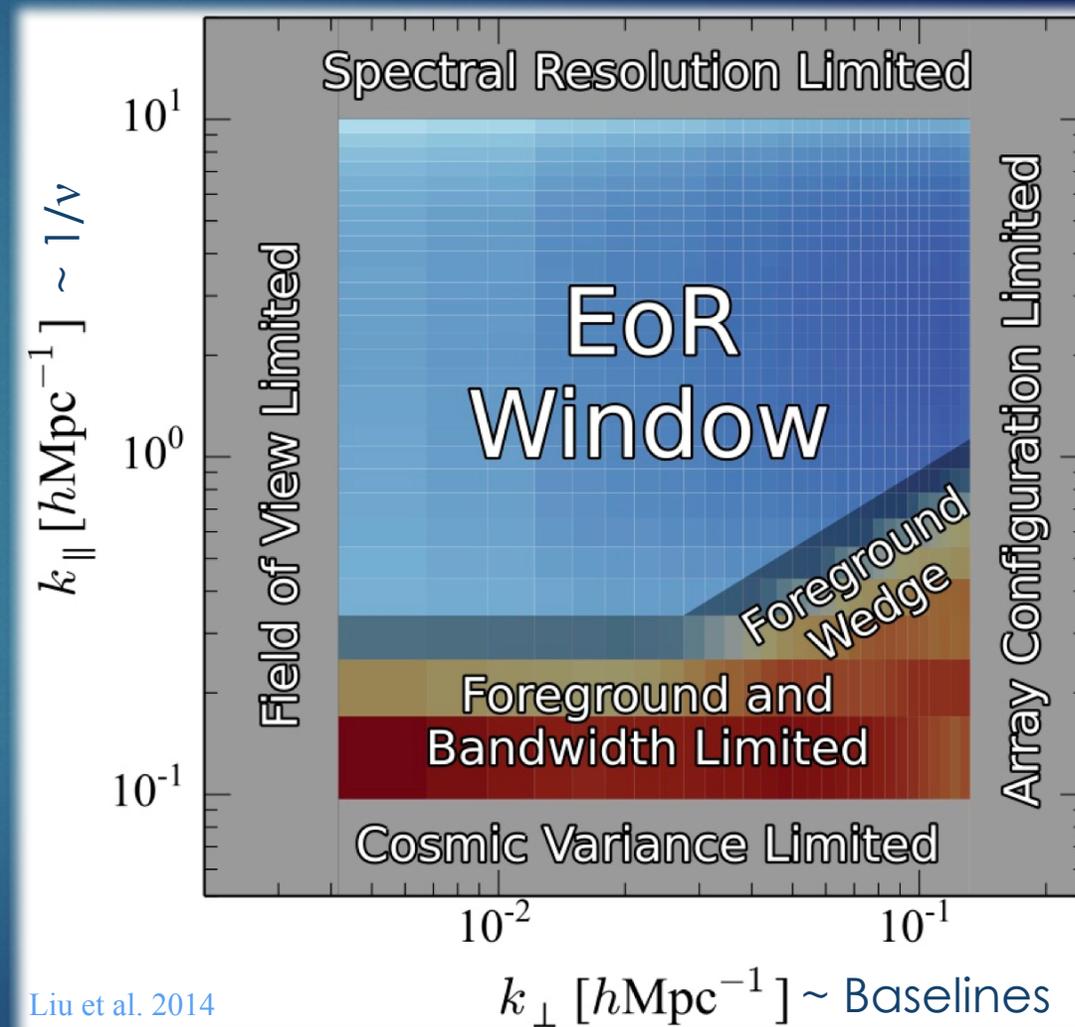
2D PS useful **diagnostic** – separates frequency- and baseline-dependent effects.

Foreground **removal** attempts to remove foregrounds and see inside the wedge.

Foreground **avoidance** ignores modes in the wedge.

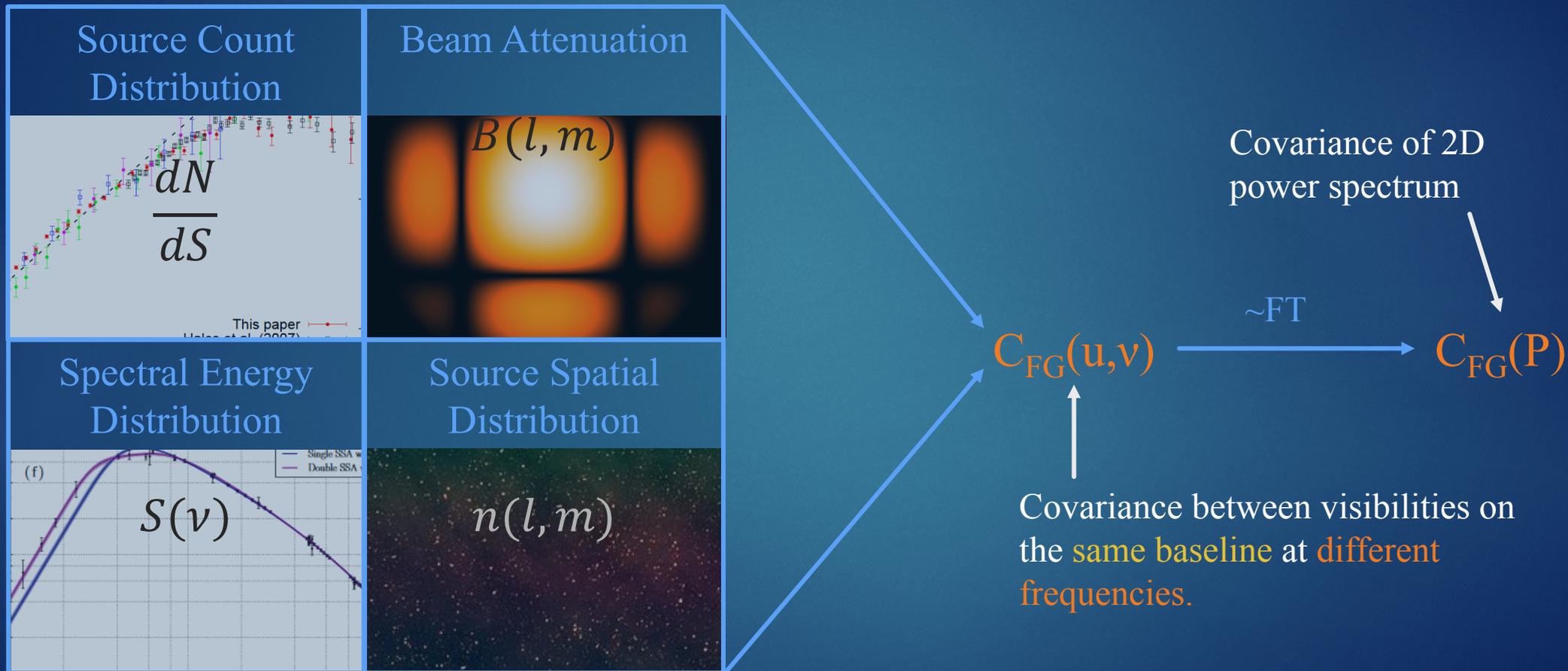
Foreground **suppression** optimally down-weights noisy modes to use *all data*, given a *model covariance* from *residual* foregrounds.

(Liu+Tegmark 2011, Liu+2014a,b)



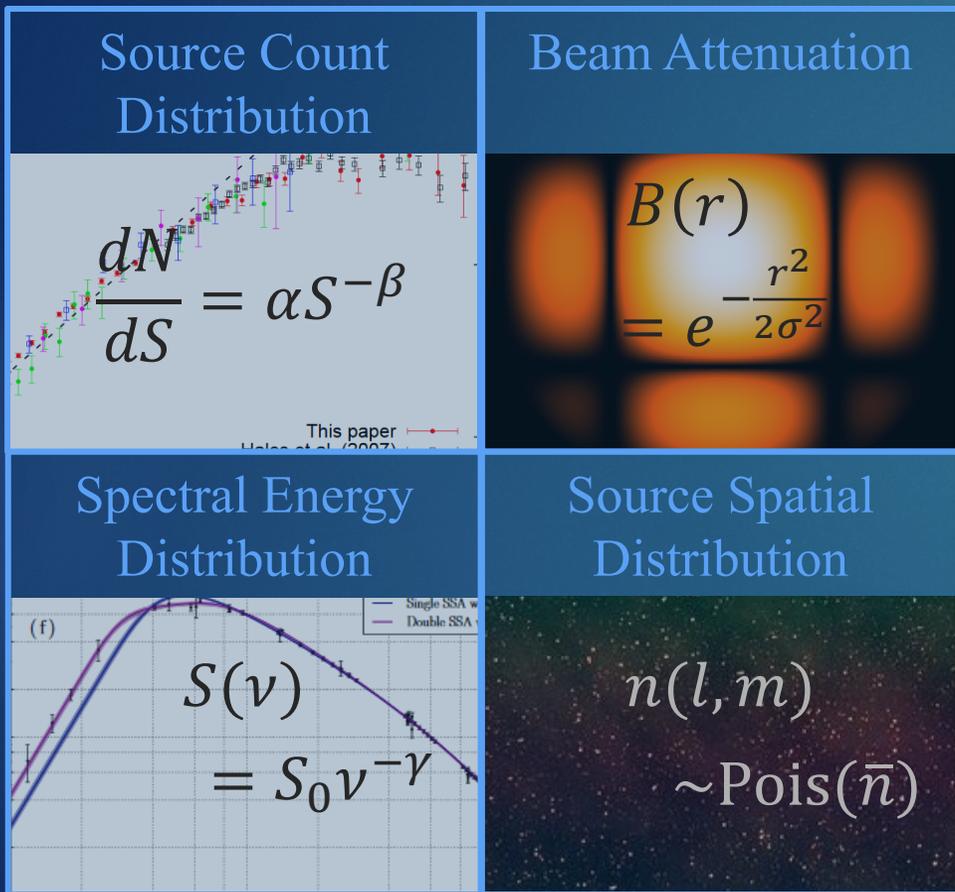
# A Framework for Statistical Point-Source Foregrounds (CHIPS)

Statistical Model Components



# Current Simple Component Models

## Statistical Model Components



Smooth frequency dependence

Exponential decay with on-sky scale

$$2\pi (f'_0 f''_0)^{-\gamma} \mu_2 \Sigma_\nu^2 \exp(-2\pi^2 u^2 f_\nu^2 \Sigma_\nu^2)$$

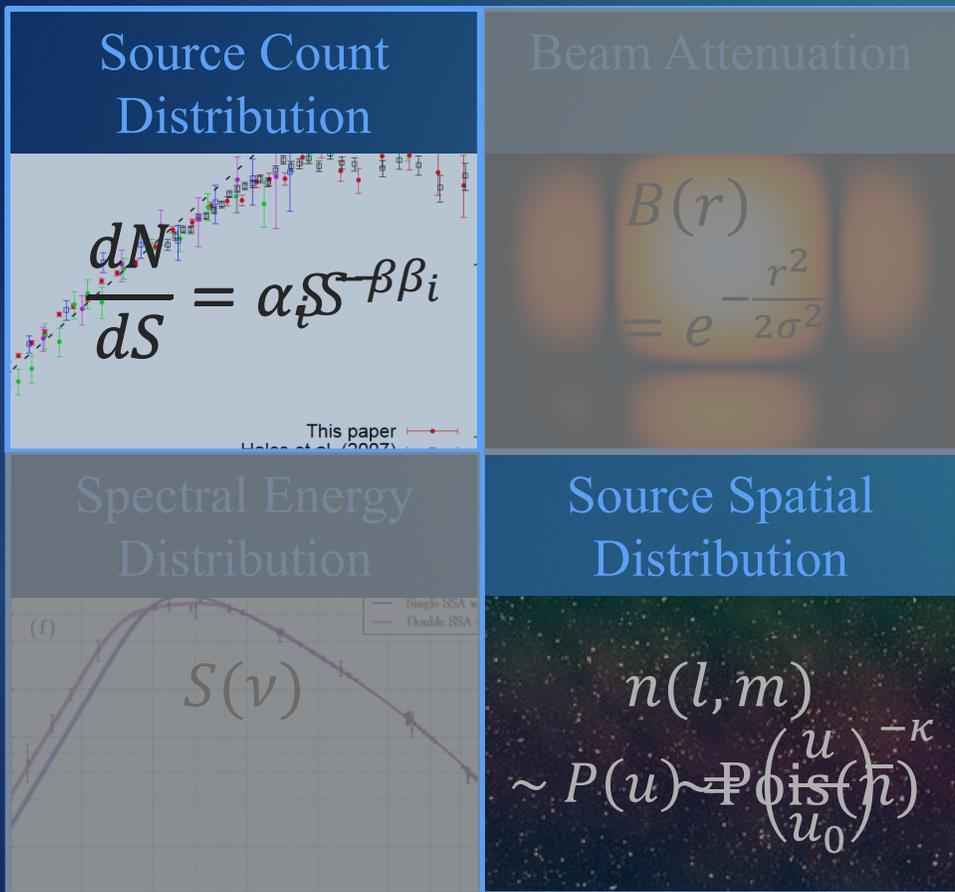
Second moment of source-count distribution

Exponential decay with frequency difference

Dependence on beam-width

# A Revised Model

## Statistical Model Components



Dependence on source spatial distribution

Beam-width dependence

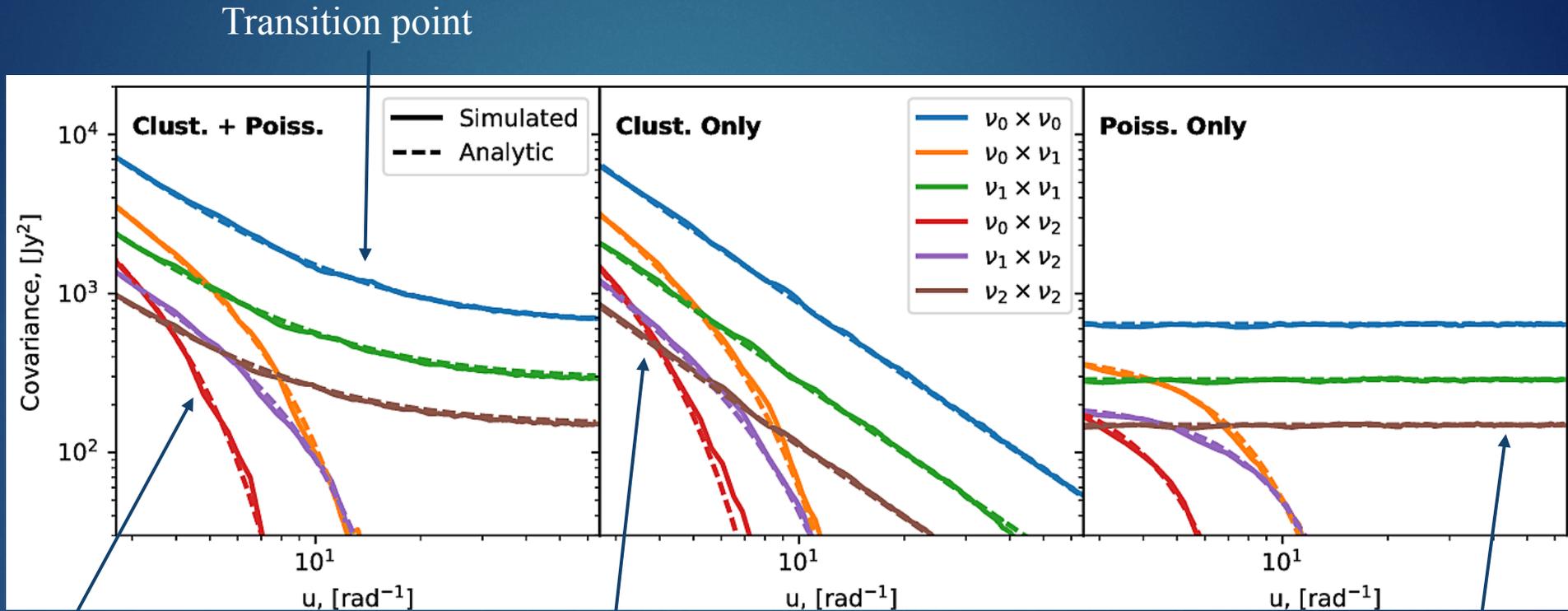
Exponential decay with on-sky scale

$$2\pi\sigma^2 \mu_1^2 \left(\frac{2\pi u}{u_0}\right)^{-\kappa} \frac{q^{-\kappa/2} (1+p^2)^{\kappa/2-1}}{f_0^{\kappa+\gamma} f_0^{2+\gamma}} e^{2\pi^2\sigma^2 u^2 (q-2)}$$

First moment of source count distribution

“Smooth” dependence on frequency

# Model Features I: *Test vs Simulation*

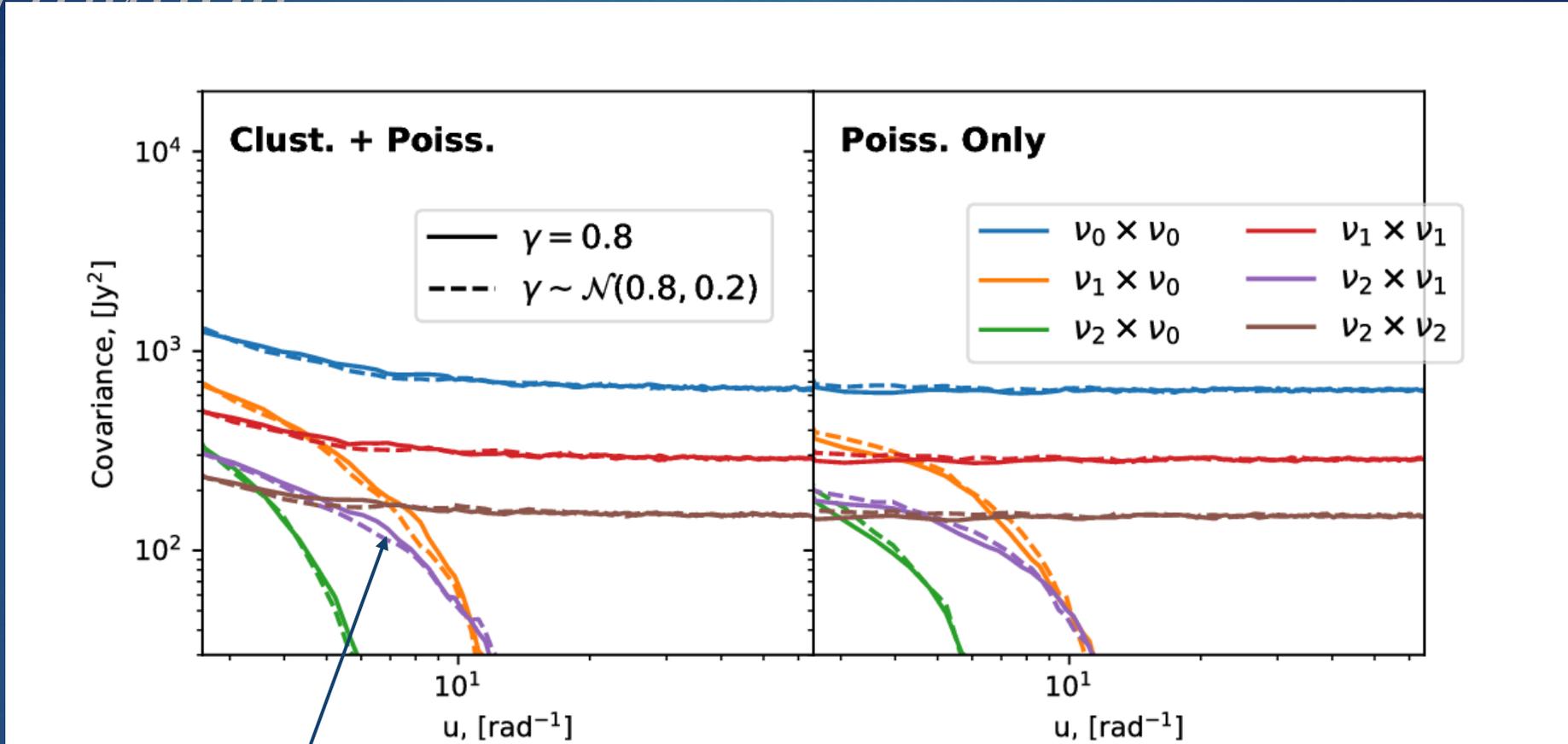


Analytic solution agrees with simulation

Clustering dominates on large scales

Poisson noise dominates on small scales

# Model Features I: *Testing Spectral Index Distribution*



Normal Dist. of Spec. Index does not change results

# Model Features II: *Source-Counts*

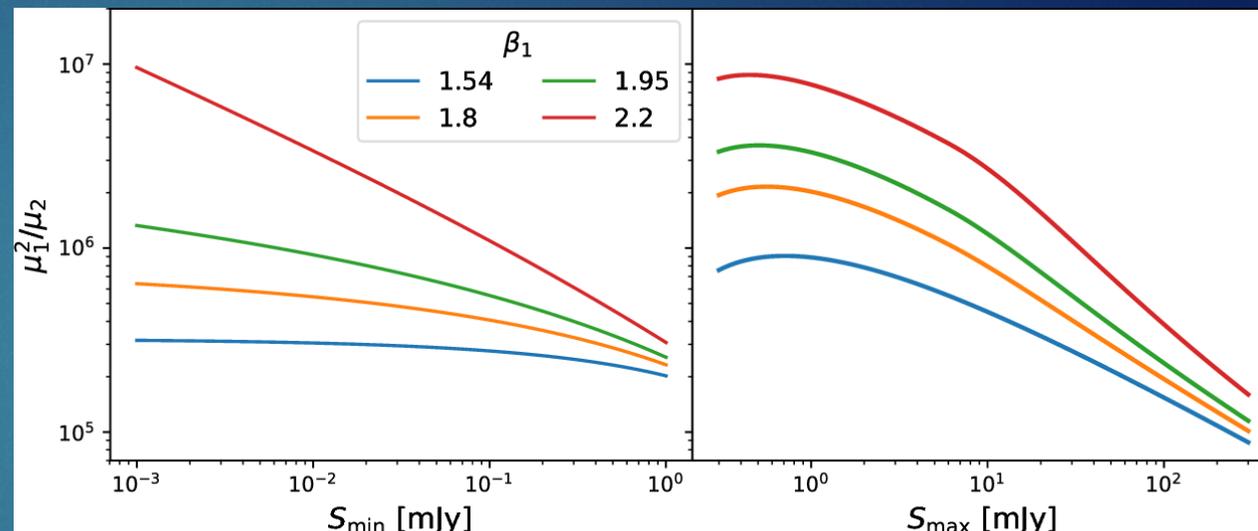
The scale above which **clustering dominates** is important:

$$u_{\star} = \left( \frac{\mu_1^2}{\mu_2} \right)^{1/\kappa} \frac{u_0}{2\pi}$$

Clustering more important if:

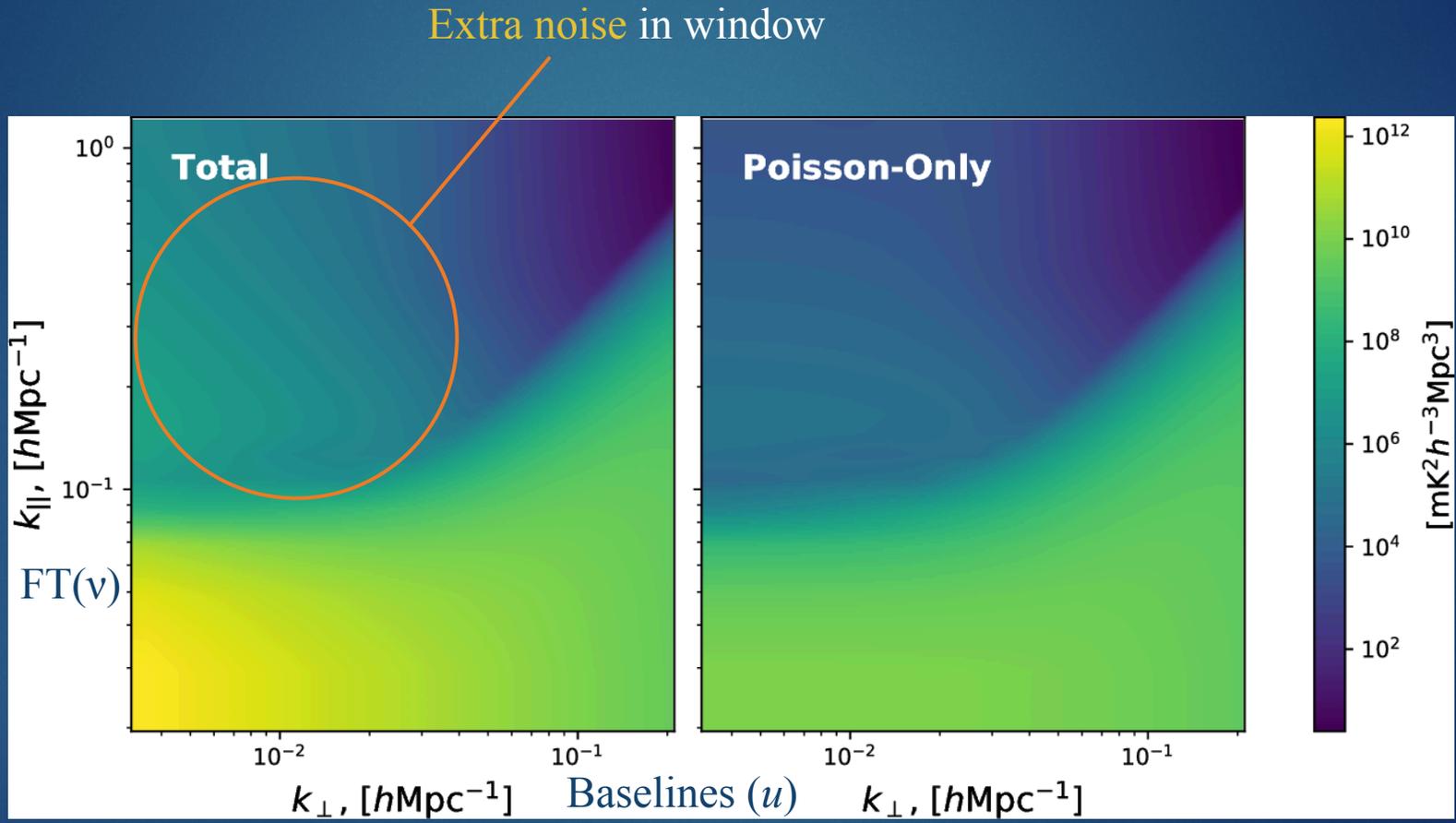
- ❖ Fainter sources exist
- ❖ More sources peeled (SKA!)
- ❖ Fainter sources more abundant

Very **large-scale-heavy** source distribution may push clustering into **unobserved scales**.

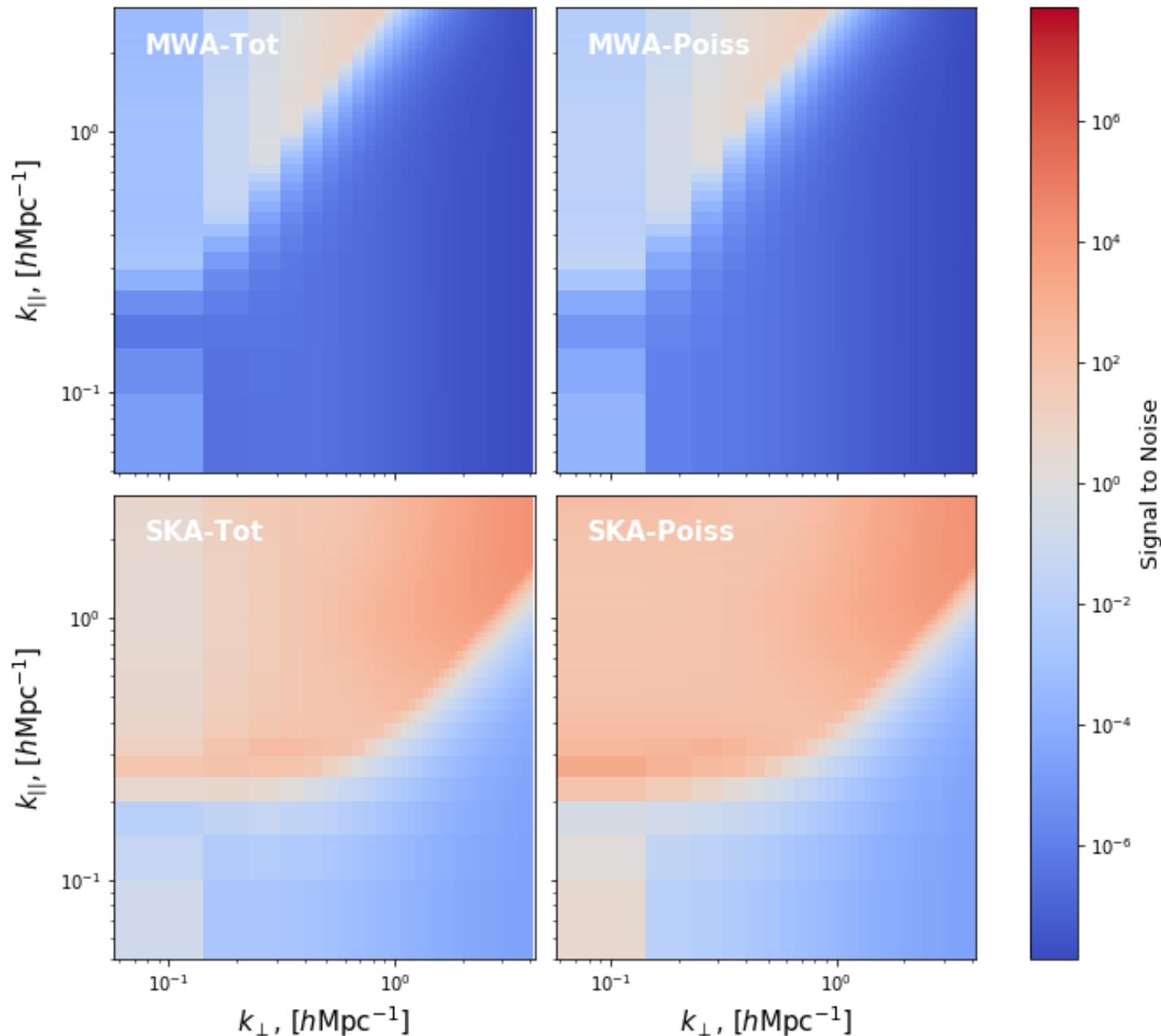


Current knowledge of the faint source population lets  $u_{\square}$  range from 13 to 5000 – from **unobservable** to **dominant** over the entire range.

# Model Features III: *Power-Spectrum Covariance*



# A Signal-to-Noise Estimate



## Fiducial Model:

$\kappa$ : 1.5 |  $u_0$ : 0.5

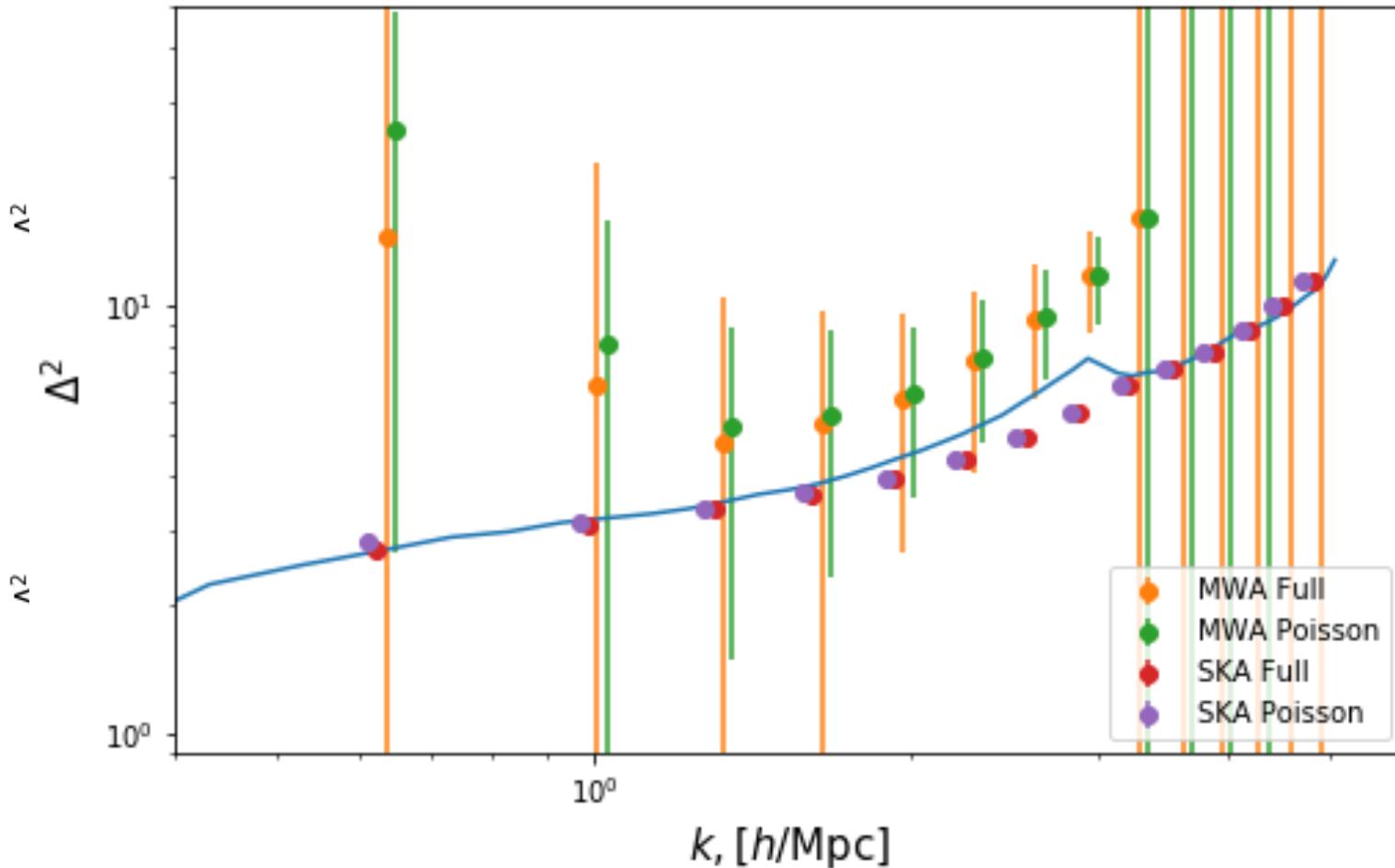
$S_{\max}$ : 30/1 mJy (MWA/SKA)

$S_{\min}$ : 0.1 mJy |  $\beta_1$ : 1.95

## Caveats!

1. Spectral/Spatial limits from **simulation**, not **instrument**.
2. Only **point-source foregrounds** present.

# Bias from Ignorance



## Fiducial Model:

$\kappa$ : 1.5 |  $u_0$ : 0.5

$S_{\text{max}}$ : 30/1 mJy (MWA/SKA)

$S_{\text{min}}$ : 0.1 mJy |  $\beta_1$ : 1.95

## Caveats!

1. Same caveats apply
2. Highly **uncertain**  $\kappa$
3. Observations more biased by **large LOS scales**.

# Limitations and Assumptions



- ▶ True only for delay-spectrum (covariance for single baseline).
- ▶ Does not yield covariance between  $u$  bins.
- ▶ Assumes all residual compact sources are point sources.
- ▶ Assumes flat-sky approximation.
- ▶ Power spectrum model not physically motivated – investigate HOD/CLF models to jointly specify source counts and clustering.
- ▶ Final results ignore galactic foregrounds, which outshine point sources on largest scales.

# Summary and Conclusions



- ❖ Biggest challenge for EoR detection is **systematic** foregrounds (more time + bigger telescope doesn't help!)
- ❖ A promising approach is to use **inverse covariance** weighting to suppress **foreground contamination**.
  - ❖ Requires **realistic** model of foreground covariances.
- ❖ We derived a new foreground covariance model **using realistic source count and spatial distributions**.
  - ❖ Realism could be enhanced by **next-generation surveys on SKA1**.
- ❖ Our model predicts:
  - ❖ **Extra covariance** on largest scales.
  - ❖ This effect grows (relatively) **stronger** for deeper surveys (i.e. **SKA!**)
  - ❖ **SKA1 (and SKA2)** will require **high-fidelity models of source clustering** to accurately predict large-scale EoR PS.

