
*Foreground Subtraction in redShifted 21cm
Global Signal experiments*

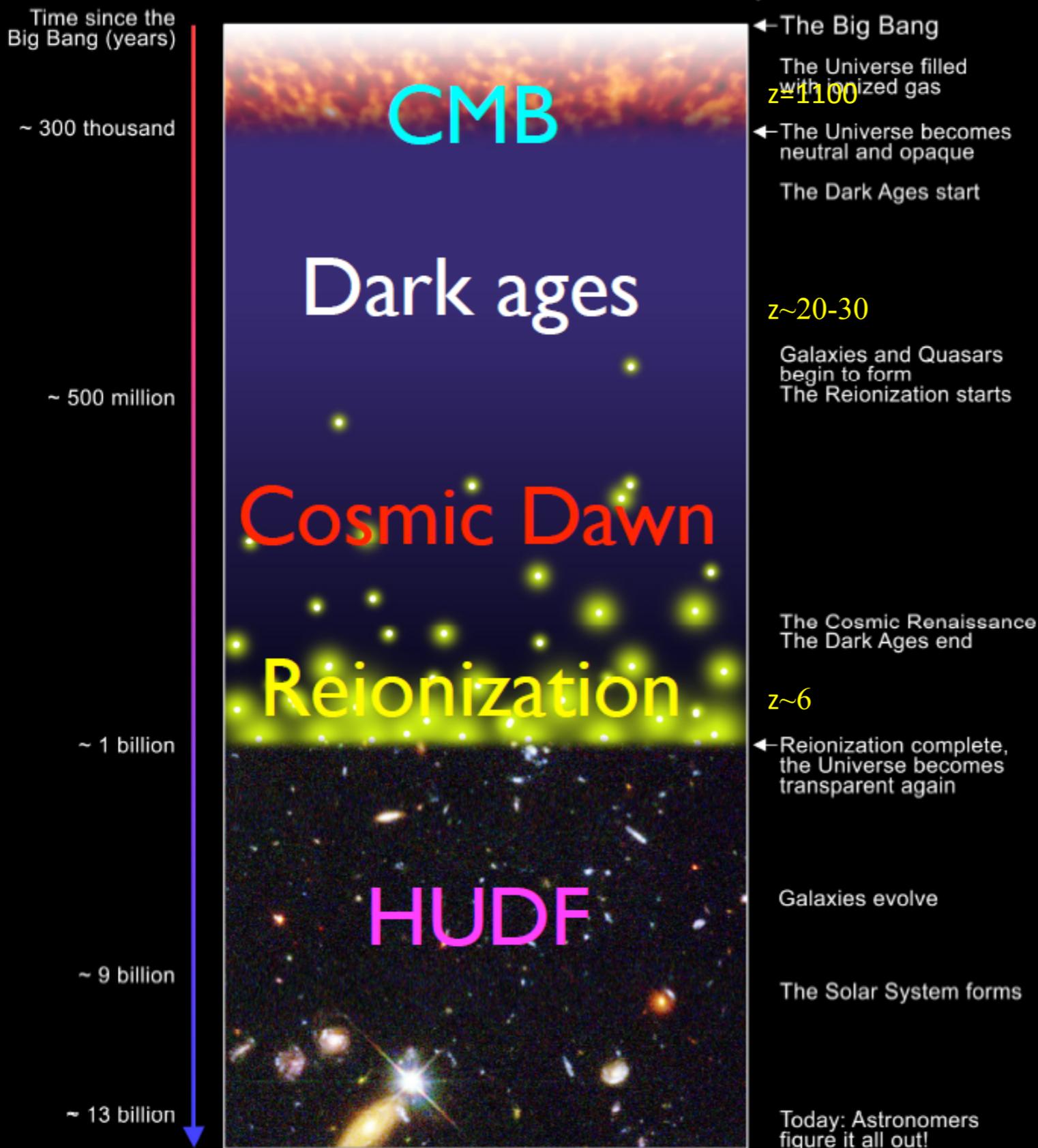
– using artificial Neural networks.

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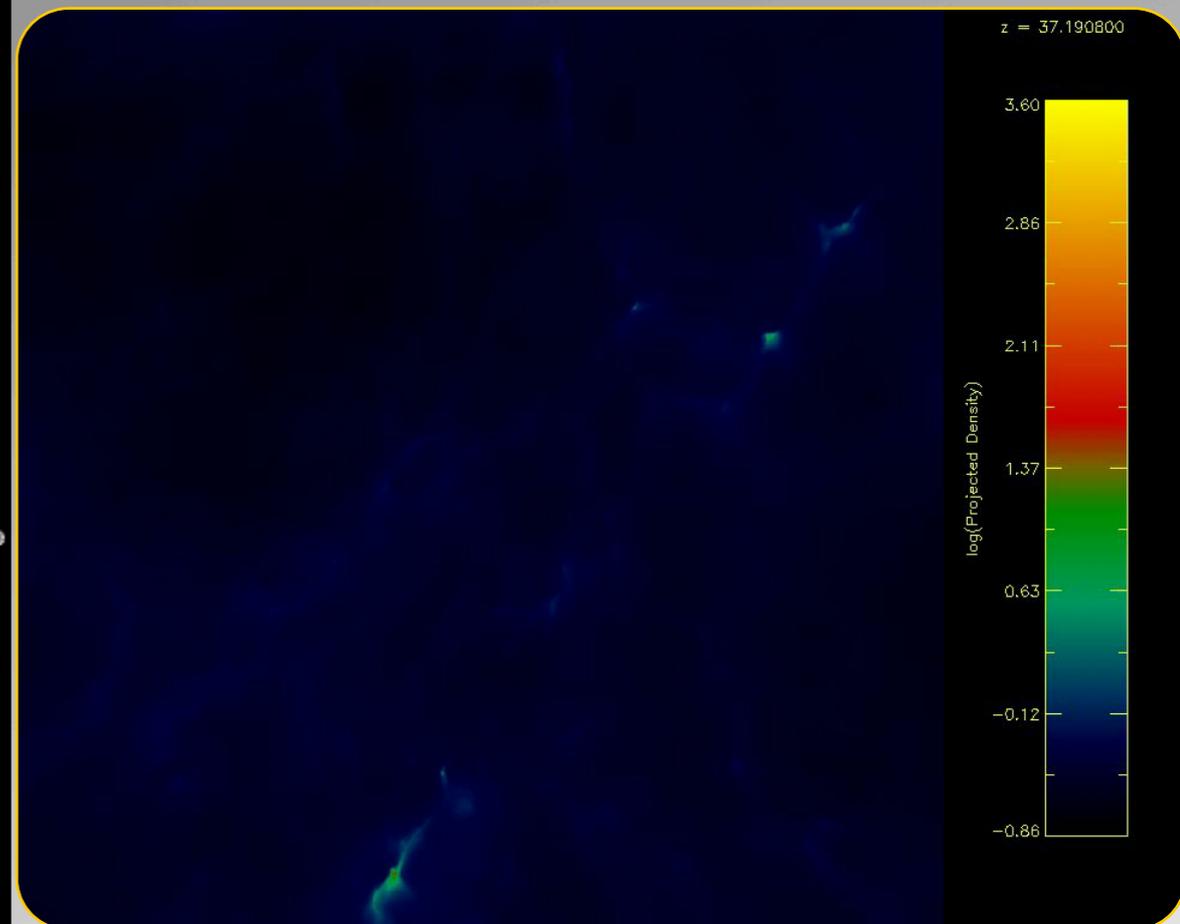


The First 0.5 Billion Years

A Schematic Outline of the Cosmic History



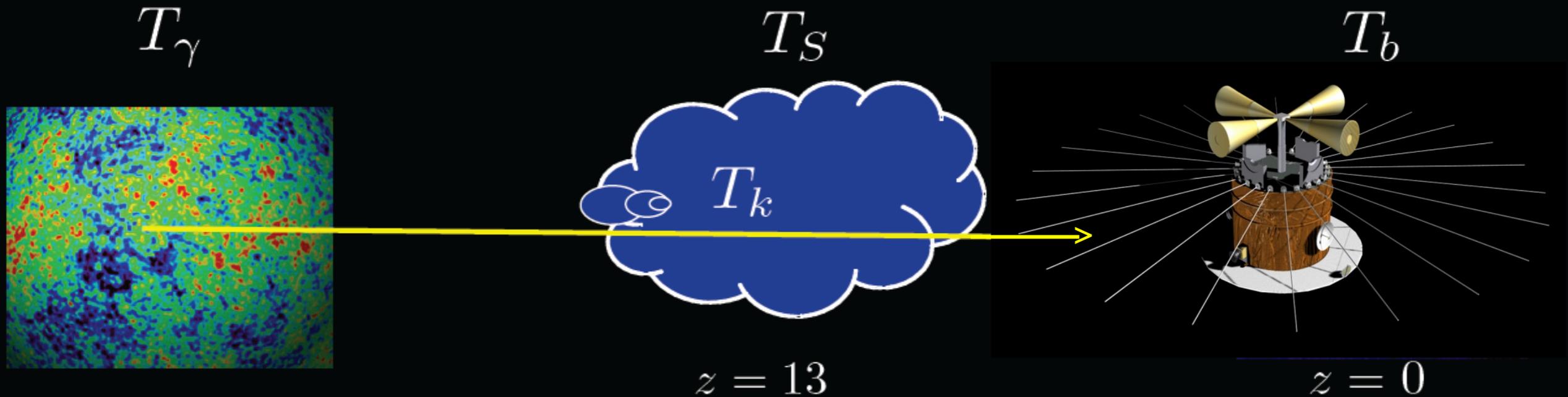
S.G. Djorgovski et al. & Digital Media Center, Caltech



The First Stars

John Wise, Georgia Tech

The 21-cm Line in Cosmology



$z = 13$
 $\nu = 1.4 \text{ GHz}$

$z = 0$
 $\nu = 100 \text{ MHz}$

CMB acts as
back light

Neutral gas
imprints signal

Redshifted signal
detected

brightness temperature $(P=kT_b\Delta\nu)$

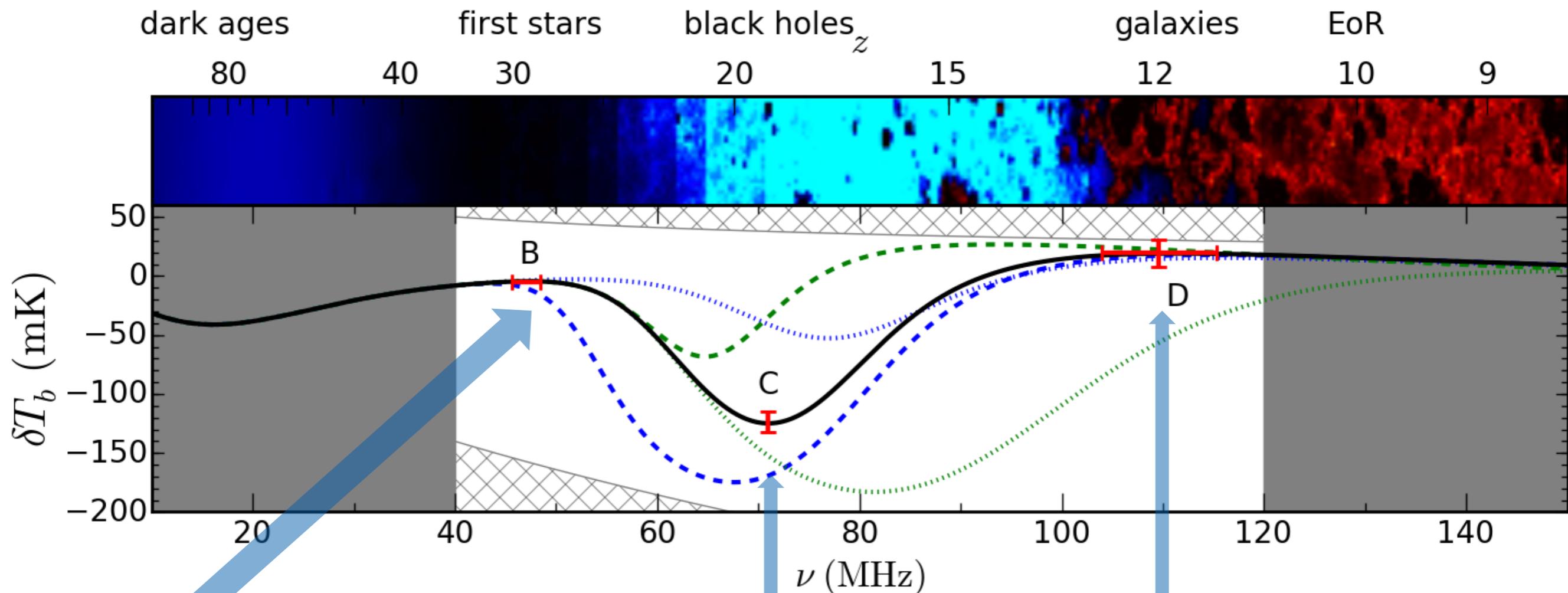
$$T_b = 27 x_{\text{HI}} (1 + \delta_b) \left(\frac{T_S - T_\gamma}{T_S} \right) \left(\frac{1+z}{10} \right)^{1/2} \left[\frac{\partial_r v_r}{(1+z)H(z)} \right]^{-1} \text{ mK}$$

Annotations in the equation:
 - **neutral fraction** (yellow arrow) points to x_{HI}
 - **baryon density** (purple arrow) points to $(1 + \delta_b)$
 - **spin temperature** (red arrow) points to $\left(\frac{T_S - T_\gamma}{T_S} \right)$
 - **peculiar velocities** (blue arrow) points to $\left[\frac{\partial_r v_r}{(1+z)H(z)} \right]^{-1}$

spin temperature set by different mechanisms:

- Radiative transitions (CMB)
- Collisions
- Wouthysen-Field effect

The 21-cm Global Signal



B: ignition of first stars

- ▶ When did the First Stars ignite?
What were these First Stars?
- ▶ What surprises emerged from the Dark Ages?

C: heating by first black holes

- When did the first accreting black holes turn on?
What was the characteristic mass?

D: the onset of reionization

- When did Reionization begin?
- ••• uncertainties in 1st star models
- ••• uncertainties in 1st black hole models

Observational Approaches for Detection of Global 21-cm Monopole

Single Antenna Radiometers

- EDGES (Bowman & Rogers)
- SARAS (Patra et al.)
- LEDA (Greenhill, Bernardi et al.)
- SCI-HI (Peterson, Voytek et al.)
- BIGHORNS (Sokolowski et al.)
- DARE (Burns et al.)

Challenges include systematics arising from stability issues, accurate calibration, polarization leakage, foregrounds.

Small, Compact Interferometric Arrays

- Vedantham et al.
- Mahesh et al.
- Presley, Parsons & Liu
- Subrahmanyan, Singh et al.

Challenges include cross-talk among antenna elements, mode-coupling of foreground continuum sources into spectral confusion, sensitivity.

FOREGROUNDS: MAJOR CHALLENGE

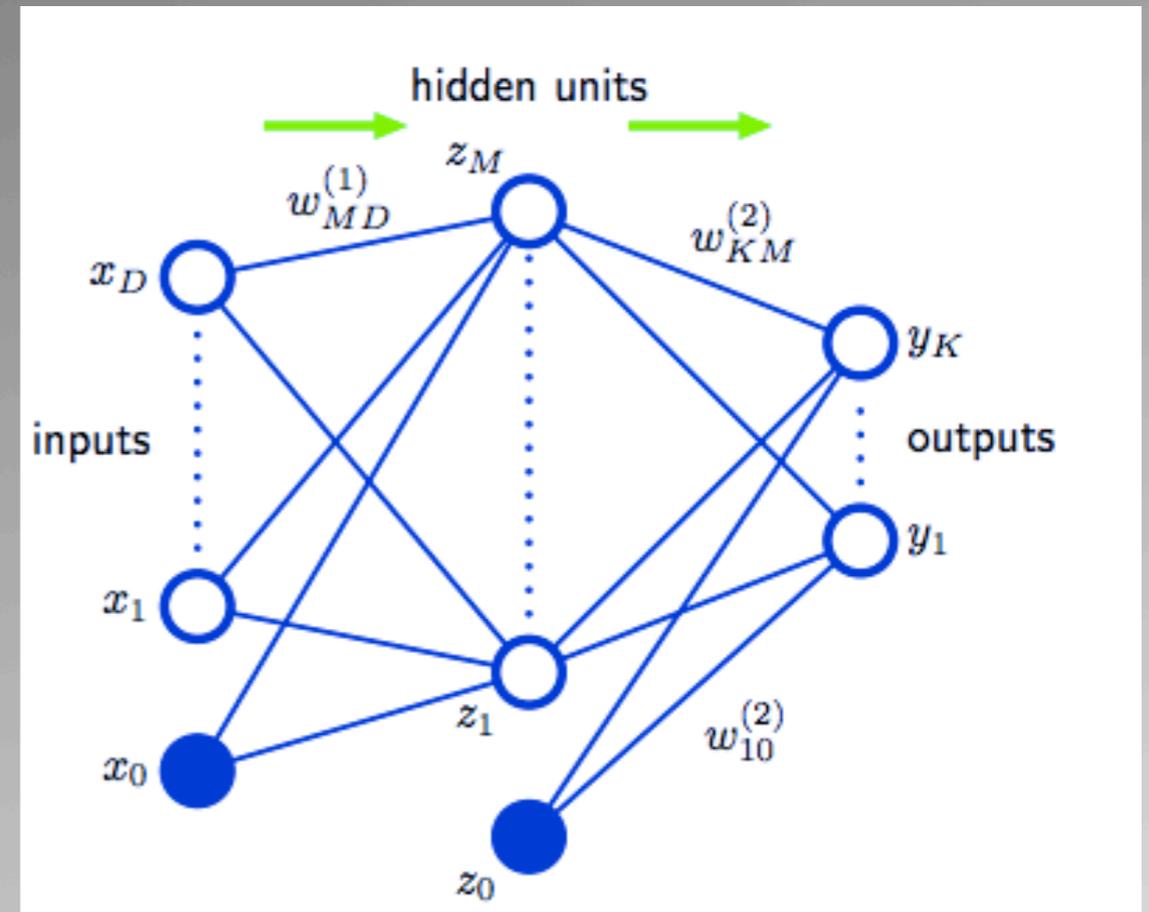
- ▶ **Earth's Ionosphere** (e.g., Vedantham et al. 2014; Datta et al. 2016; Rogers et al. 2015; Sokolowski et al. 2015)
 - Refraction, absorption, & emission
 - Spatial & temporal variations related to forcing action by solar UV & X-rays => 1/f or flicker noise acts as another systematic or bias.
 - Effects scale as ν^{-2} so they get much worse quickly below ~ 100 MHz.
- ▶ **Radio Frequency Interference (RFI)**
 - RFI particularly problematic for FM band (88-110 MHz).
 - Reflection off the Moon, space debris, aircraft, & ionized meteor trails are an issue everywhere on Earth (e.g., Tingay et al. 2013; Vedantham et al. 2013).
 - Even in LEO (10^8 K) or lunar nearside (10^6 K), RFI brightness T_B is high.
- ▶ **Galactic/Extragalactic**
 - Mainly synchrotron with expected smooth spectrum ($\sim 3^{\text{rd}}$ order log polynomial,
$$\log T_{\text{fg}} = \sum_{i=0}^{N_{\text{poly}}} a_i \log \left(\frac{\nu}{\nu_0} \right)^i$$
, although it is corrupted by antenna beam; e.g., Bernardi et al. 2015).
EDGES finds spectral structure at levels < 12 mK in foreground at 100-200 MHz.

ARTIFICIAL NEURAL NETWORK

- ▶ These are machine learning algorithms which mimics the functioning of our brains.
- ▶ By feeding the network, enough amount of training data, the network can be trained to perform a certain task.
- ▶ You must have noticed how efficiently Google predicts your search queries as you begin typing your query in the search box. This is a very common application of pattern recognition techniques being used today.
- ▶ Further applications are seen in biometrics, gene-replication research, efficient compression of sequential files, etc.
- ▶ More recent works in HI Cosmology, Gravitational Lens, etc

Structure of the Network

- ▶ Input layer : We provide the training dataset to the input neurons.
- ▶ Hidden layer: The inputs are assigned weights and then activated using an activation function.
- ▶ Output layer: The information from the hidden layer is passed on to the output layer again by assigning weights.
- ▶ Training: The weights are adjusted so as to minimise the cost function, using the back-propagation algorithm.
- ▶ This is an iterative process, which assigns a different weight to each input till the cost function converges.



Using the framework in

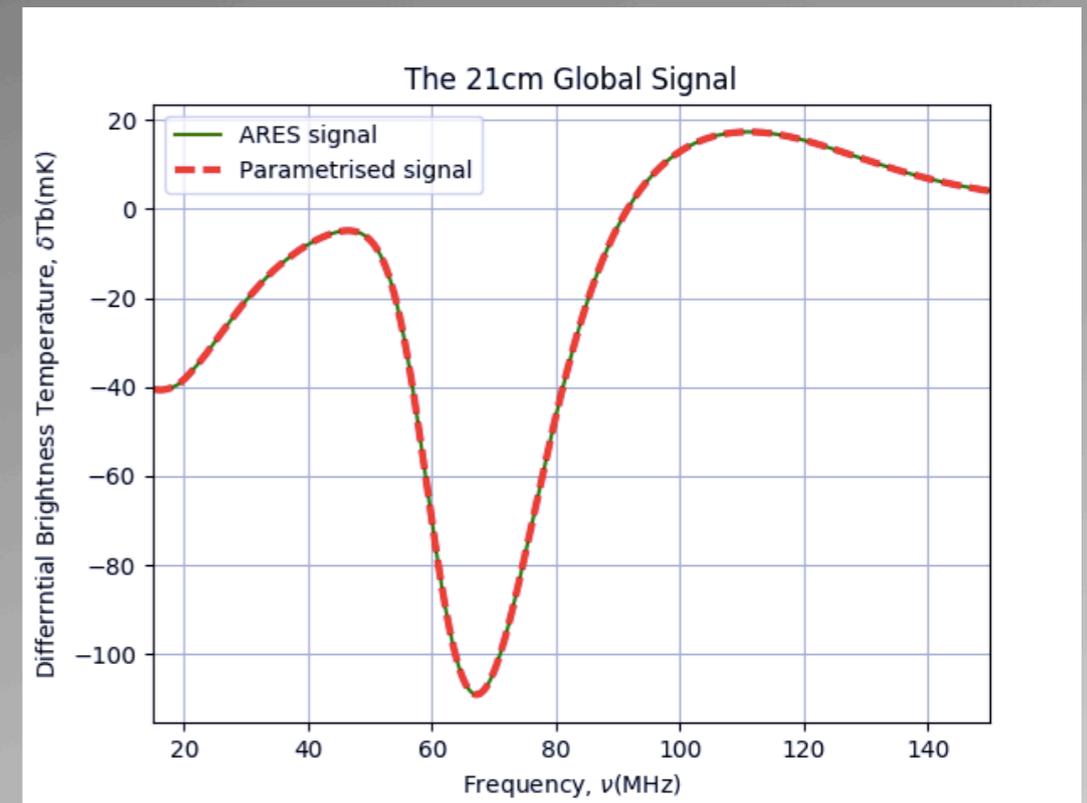
KERAS package : <https://keras.io/>

MODEL GLOBAL 21CM SIGNAL

- ▶ We use the Accelerated Reionization Era Simulations (ares) code was designed to rapidly generate models for the global 21-cm signal (Mirocha et al, 2012, 2015).
- ▶ We have used the tanh model for parametrising the global signal, where the parameters , $A(z)$ are the parameters for the global signal.

$$A(z) = \frac{A_{\text{ref}}}{2} \{1 + \tanh[(z_0 - z)/\Delta z]\}$$

- ▶ The following plot shows the simulated signal from ARES and the calculated result for the signal.



PARAMETERS evolve according to a tanh model

- ▶ $J(z)$ —Lyman-alpha background(which determines the strength of W-F coupling)
- ▶ $X_i(z)$ — Ionized fraction of hydrogen
- ▶ $T(z)$ —temperature of the IGM

FOREGROUND MODEL

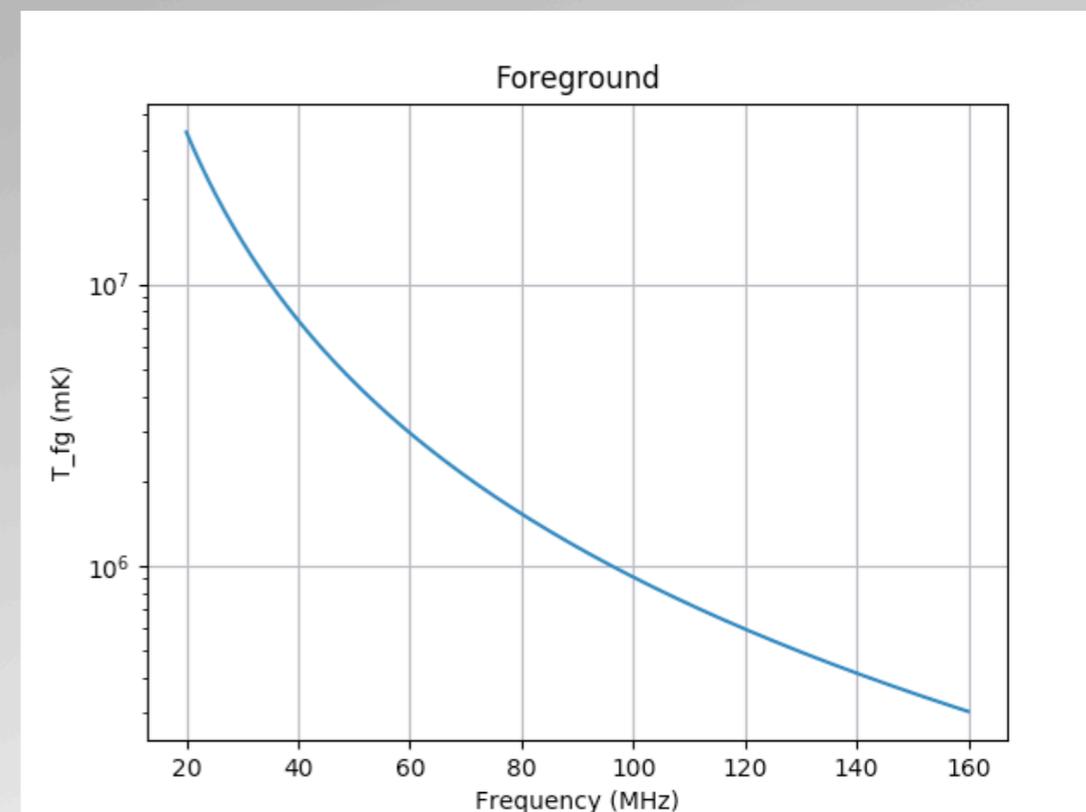
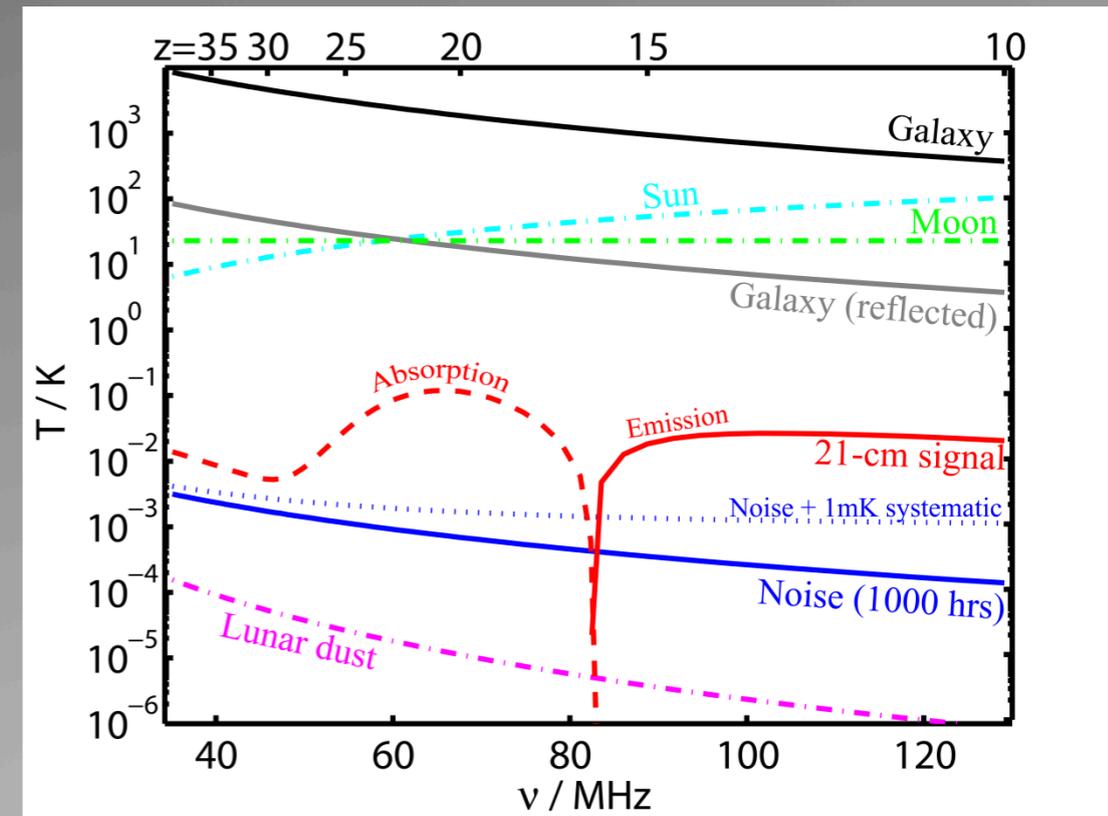
- ▶ The foreground model used is of the form:

$$\log T_{\text{FG}}^i = \log T_0^i + a_1^i \log(\nu/\nu_0) + a_2^i [\log(\nu/\nu_0)]^2 + a_3^i [\log(\nu/\nu_0)]^3,$$

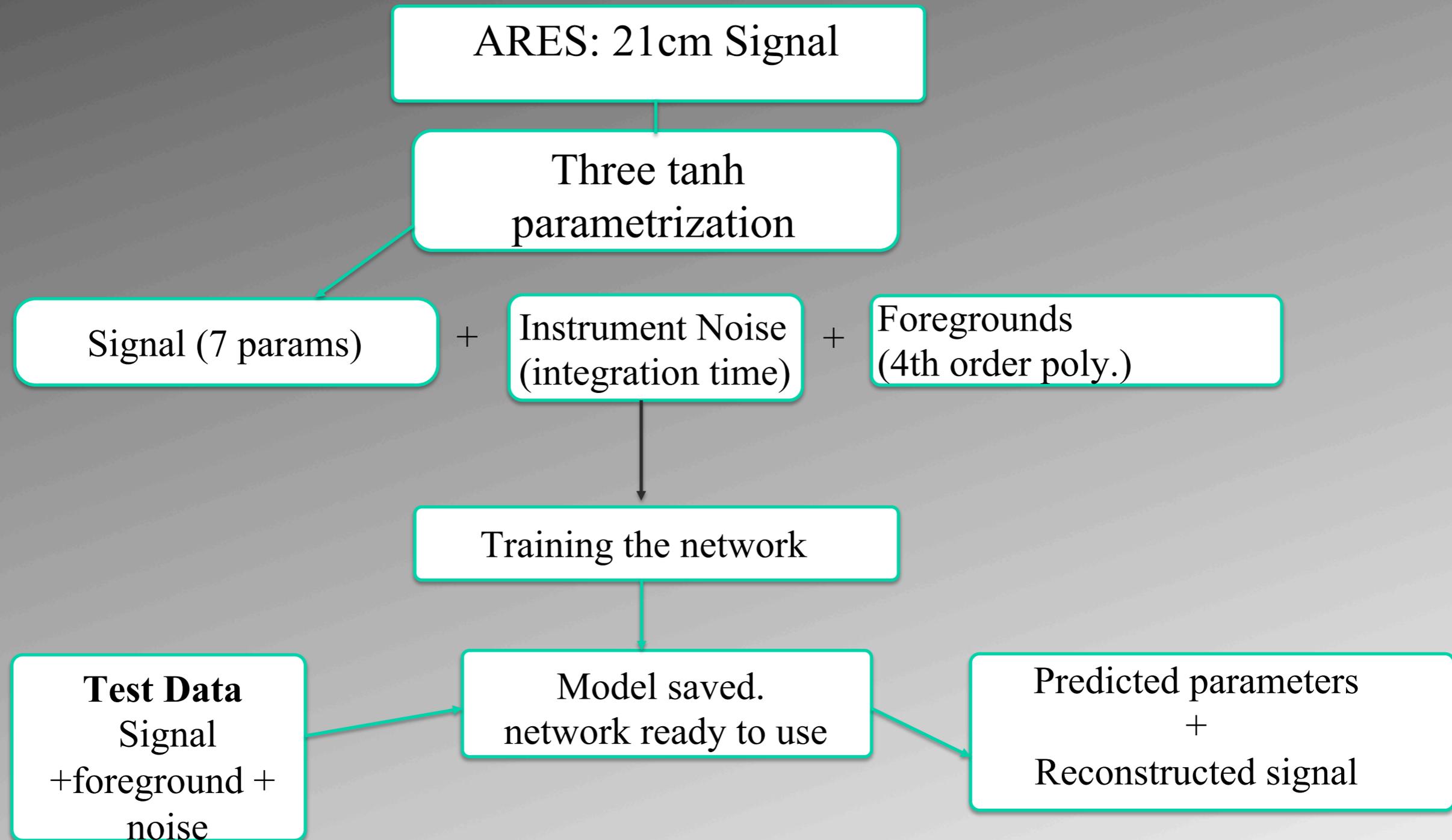
$$\nu_0 = 80$$

Foreground parameters

- ▶ $a_0 = (\log T_0)$, a_1, a_2, a_3
- ▶ Where, all temperatures are in K, and Hz, is an arbitrary reference frequency, which is chosen to lie in the middle of our band.



OUTLINE

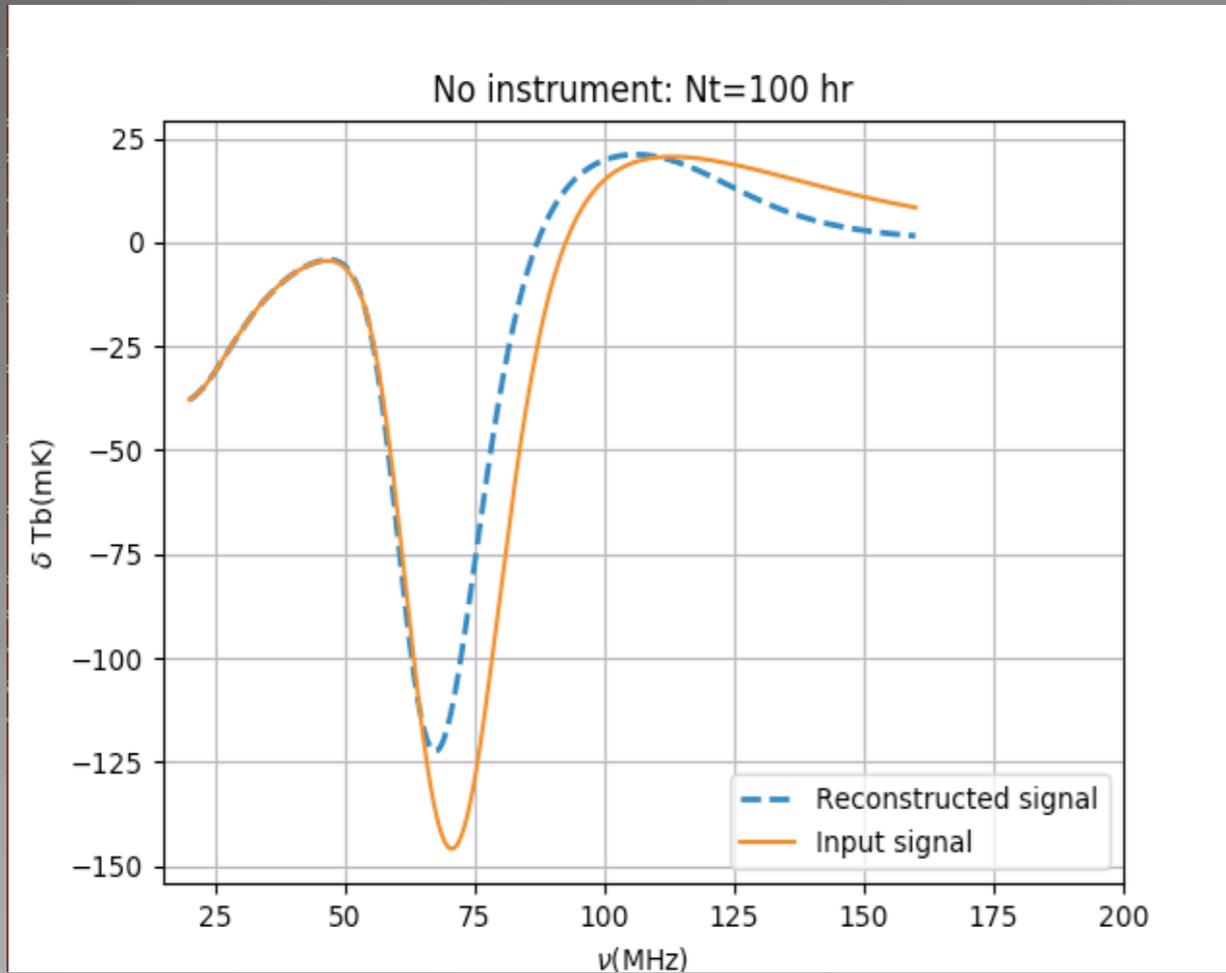


Training the Network

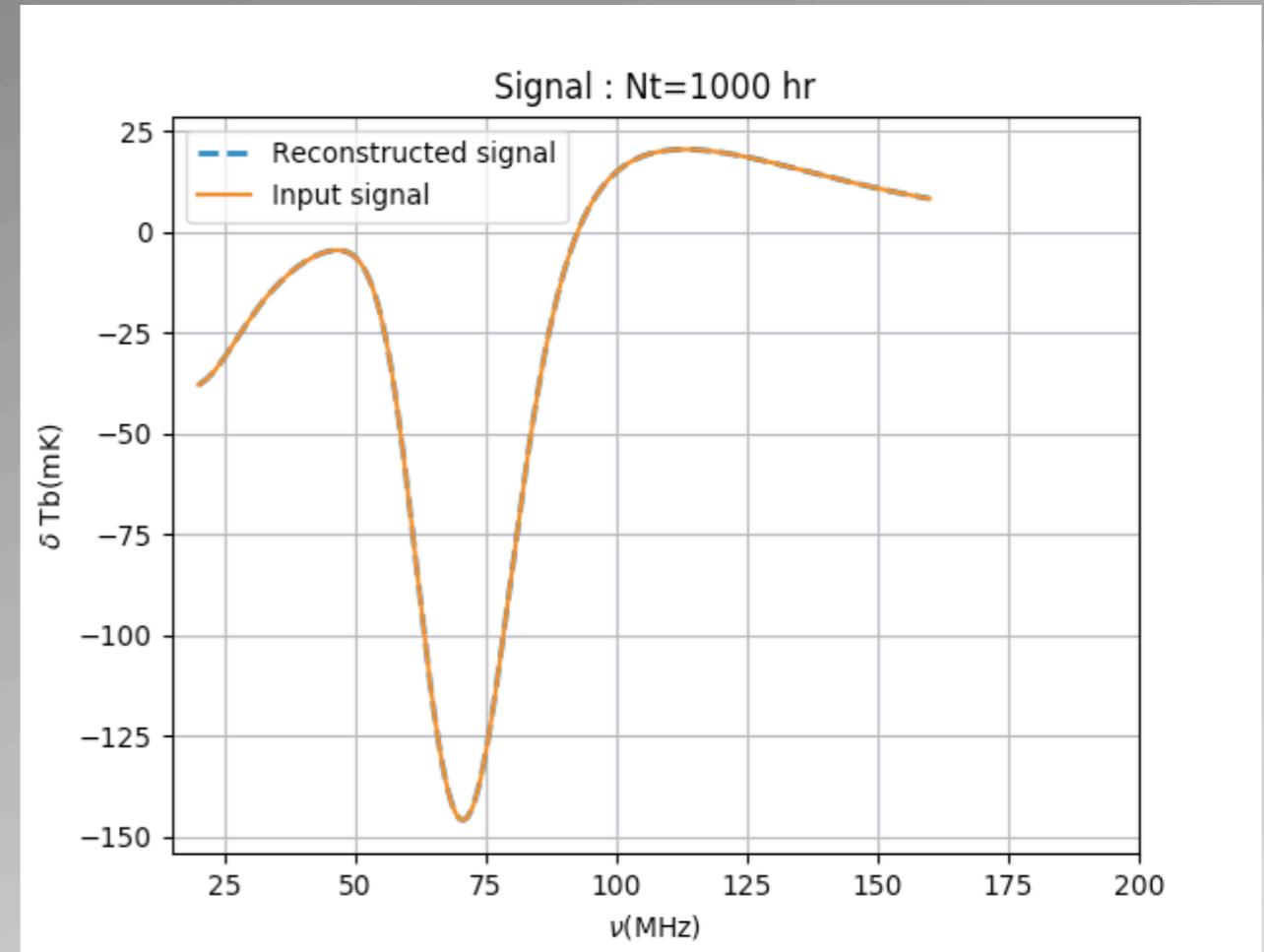
- ▶ We have generated 2500 datasets for input to the network, which was then split into training (70%) and the testing datasets(30%).
- ▶ Each dataset has 1024 frequency channels (20,160) MHz, i.e. $Z \sim (70, 8)$.
- ▶ The network is trained with thermal noise and with/without instrument response.
- ▶ We have used an ANN with a single hidden layer with 15-18 neurons, and there are 11-13 output neurons corresponding to the 11-13 parameters.

Simulations

► Case 1: 21CM Signal + Foreground + Instrumental Noise



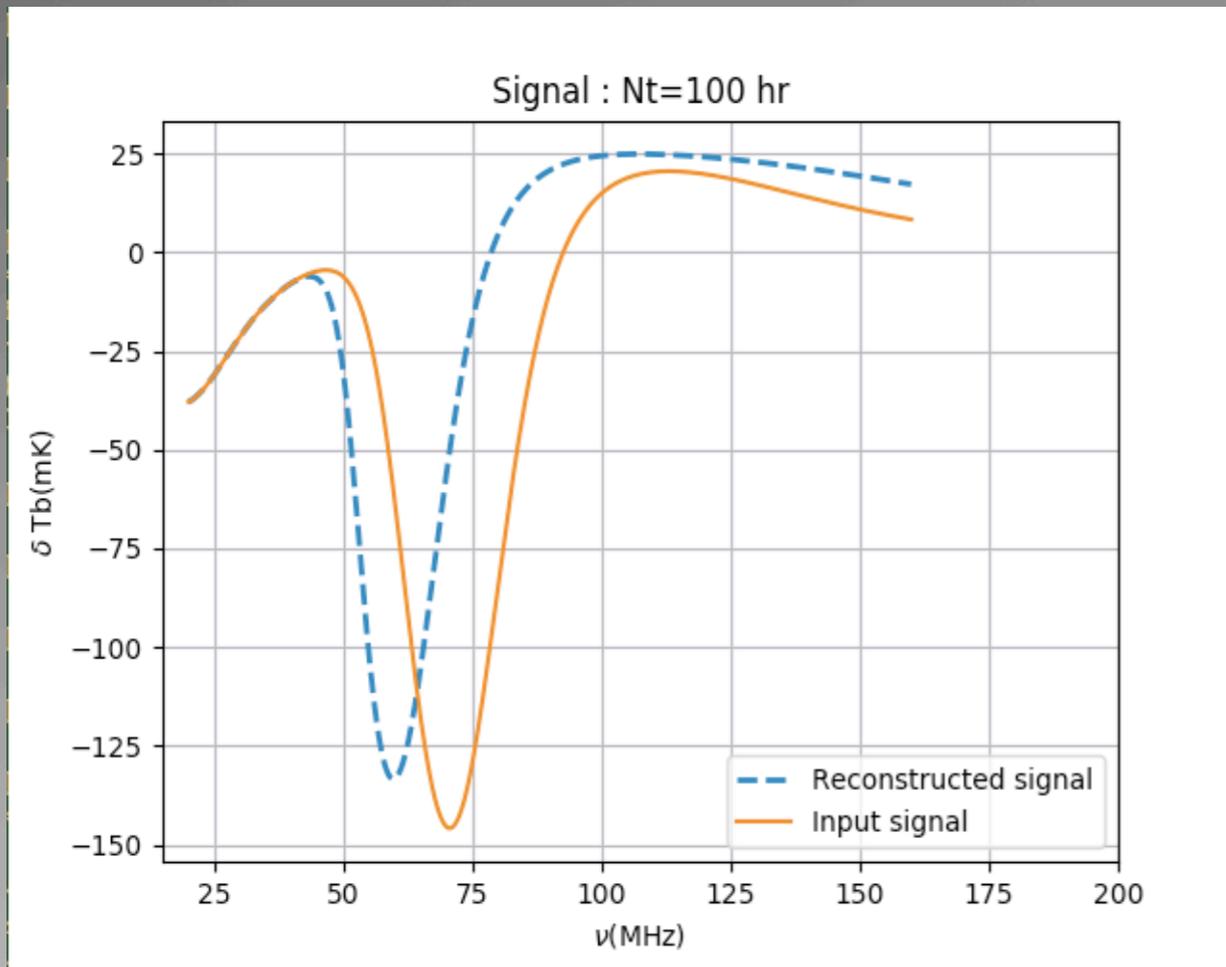
RMSE on Jref = 8 %



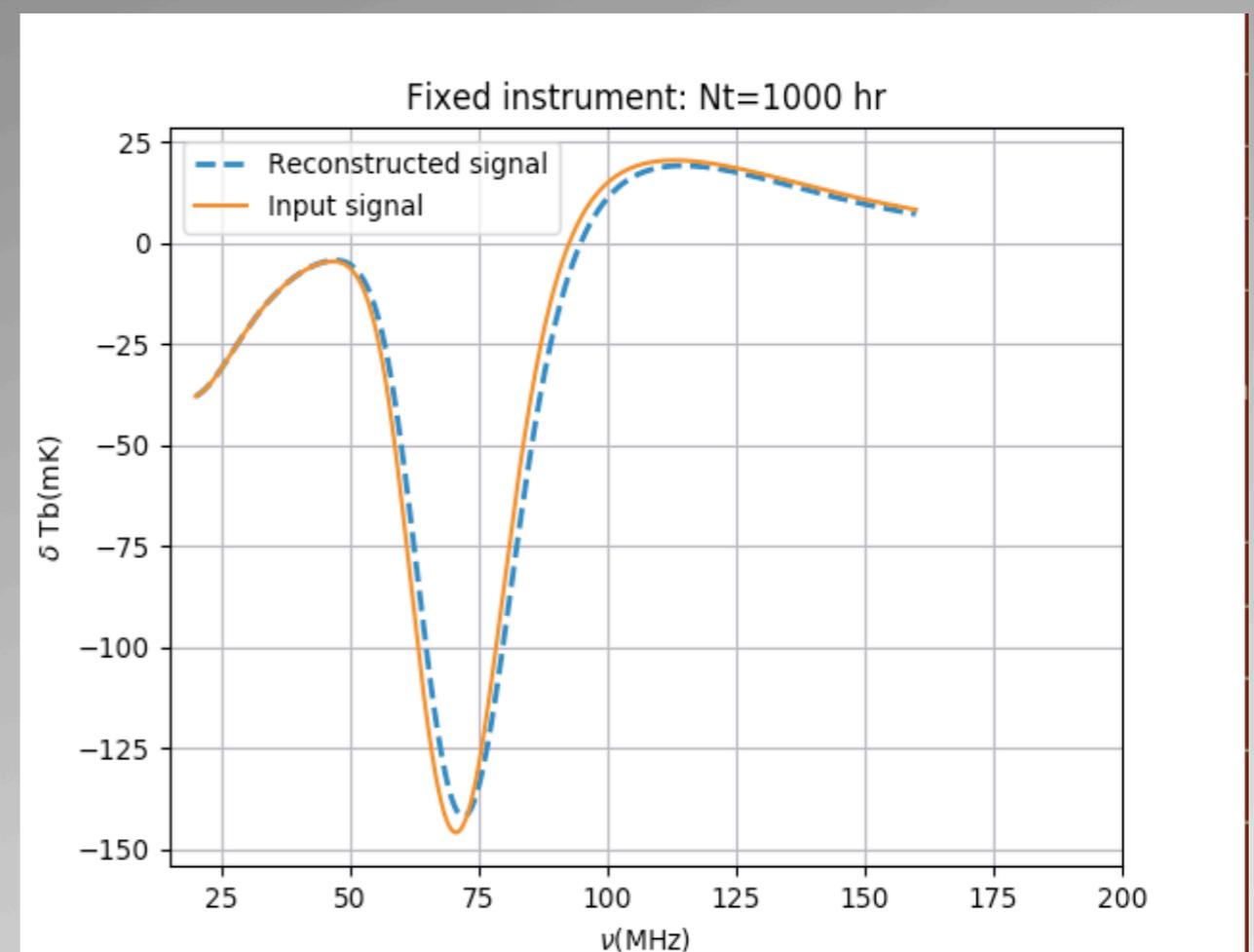
RMSE on Jref = 3 %

Simulations

- ▶ Case 2: 21CM Signal + Foreground + Instrumental Noise + Instrumental Gain (Bandpass) fixed over time



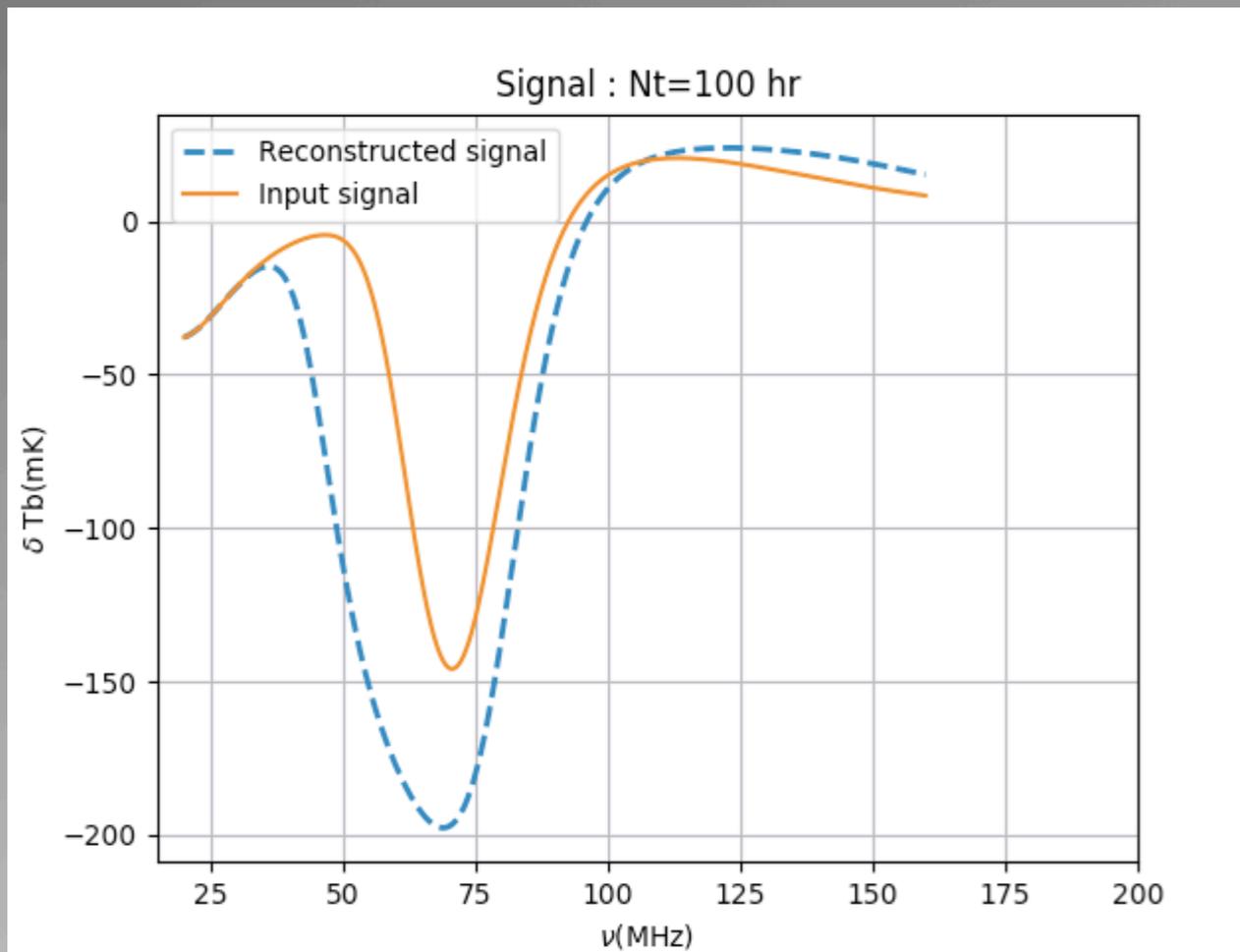
RMSE on Jref = 20 %



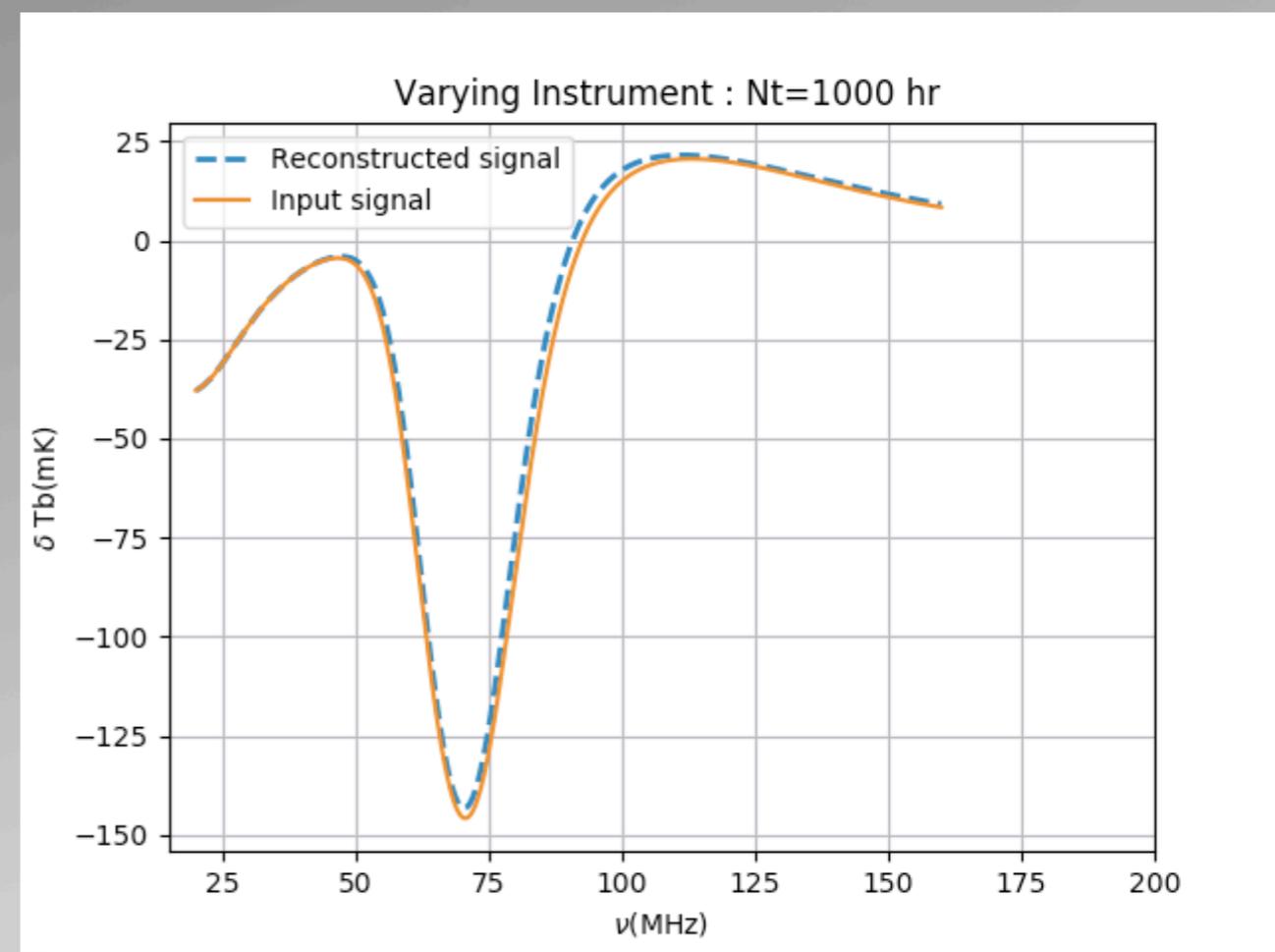
RMSE on Jref = 5 %

Simulations

- ▶ Case 3: 21CM Signal + Foreground + Instrumental Noise + Instrumental Gain (Bandpass) varying over time



RMSE on Jref = 38 %



RMSE on Jref = 13 %

Way Forward

- ▶ ANN seems to be a new flavor ..
- ▶ Alternate to MCMC - complimentarity ??
- ▶ Further simulations - Global and PS